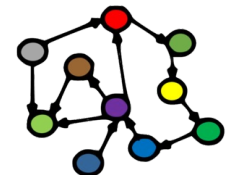


Welcome to INFO216:
Knowledge Graphs
Spring 2024

Andreas L Opdahl
<Andreas.Opdahl@uib.no>

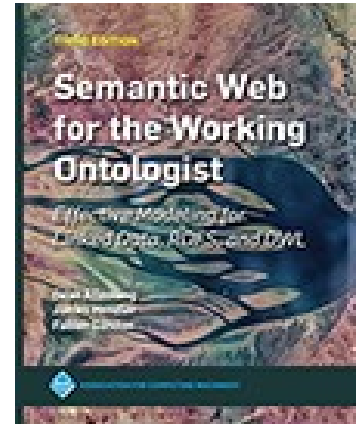
Session 9: Ontologies (OWL)

- Themes:
 - what and why?
 - basic OWL constructs (“RDFS-Plus”):
 - more precise properties
 - sameness and difference
 - complex classes
 - more advanced OWL
 - restriction classes
 - Programming in RDFLib



Readings

- Sources:
 - **Allemang, Hendler, Gandon (2020):**
Semantic Web for the Working Ontologist, 3rd edition:
chapter 9-10 (“RDFS Plus”, chapters 8-9 in the 2nd ed.)
advanced: chapters 12-13 (chapters 11-12 in the 2nd ed.)
 - Blumauer & Nagy (2020):
Knowledge Graph Cookbook – Recipes that Work:
e.g., pages 105-109, 123-124, (*supplementary*)
- Resources in the wiki <http://wiki.uib.no/info216>:
 - OWL 2 Primer, sections 2-6 (*advanced*: 9-10):
<http://www.w3.org/TR/owl-primer/>
 - **show**: Turtle
 - VOWL: Visual Notation for OWL Ontologies

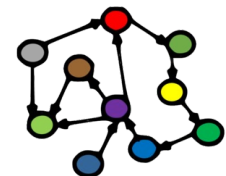


THE KNOWLEDGE GRAPH
COOKBOOK
RECIPES THAT WORK



ANDREAS BLUMAUER
AND HELMUT NAGY

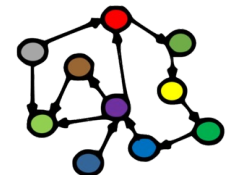
1st edition, 2020



Web Ontology Language (OWL)

Why do we need vocabularies?

- Shared, well-defined terms (dereferencable URIs) for types, properties and some individuals that can be used to represent a domain
- Domains can be:
 - people, their friends and workplaces (FOAF, BIO)
 - electronic and other documents (DC, BIBO)
 - commerce (schema.org)
 - classification in libraries etc. (SKOS)
 - general encyclopedic information (DBpedia, Wikidata)
 - general time and place (OWL-Time, geo)
 - ...and *lots* of others (→S10)



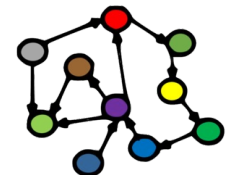
Why do we need vocabularies?

- To make knowledge graphs more precisely defined
- To make semantic data sets easier to use
 - encourage reuse
 - avoid misunderstandings and errors
 - easier to understand, recombine, enrich...
- To support computer processing
 - more powerful
 - more general



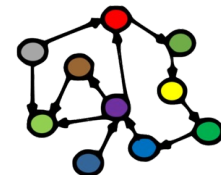
RDFS is a useful starting point...

- We can say:
 - “a president is a politician” so that
 - saying “Trump is a president” entails saying “Trump is a politician”
 - “a politician is a human” so that
 - saying “Trump is a president” *also* entails saying “Trump is a human”
 - “the president of something is a politician” so that
 - saying “Trump is a president of U.S.A.” entails “saying Trump is a politician”
 - “something having a president is a country” so that
 - saying “Trump is a president of U.S.A.” entails saying “U.S.A. is a country”
 - “being president also means being citizen” so that
 - saying “Trump is a president of U.S.A.” entails saying “Trump is a citizen of U.S.A.”
- *RDFS expresses this but not (so much) more...*



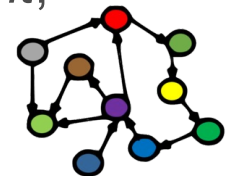
RDFS is a useful starting point...

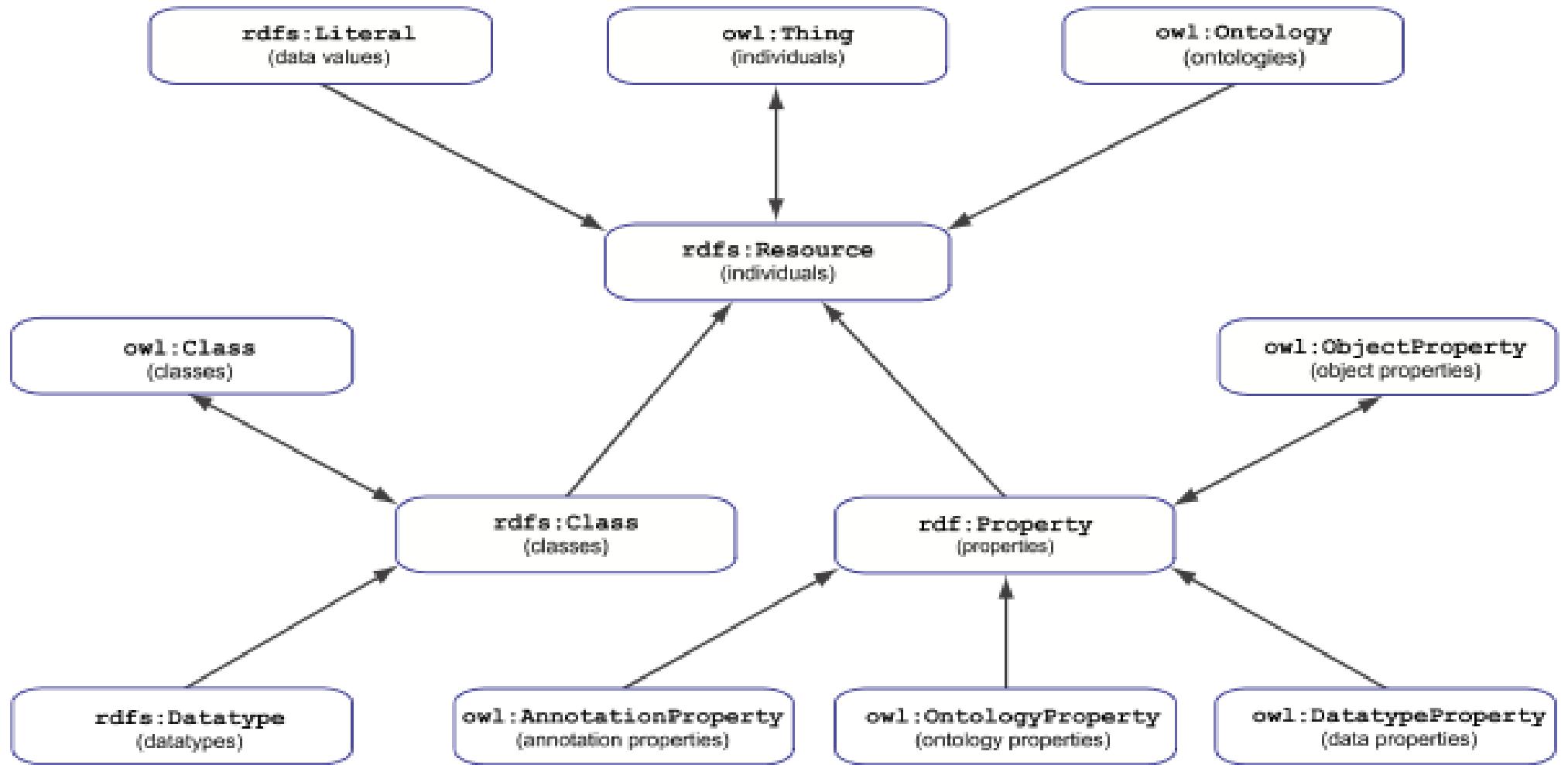
- But lots of simple stuff it cannot express, e.g.:
 - “every ancestor of an ancestor is an ancestor too”
 - “the BirthNumber of a Person is unique”
 - “a Republic has exactly one President”
 - “a FootballTeam has 11 activePlayers, a VolleyballTeam 6”
 - “a StringQuartet has two violins but only one viola and one cello”
 - “classes with different URIs actually represent the same class”
 - “resources with different URIs represent the same resource”
 - “properties with different URIs are actually the same”
 - “two individuals are different”, “two classes are disjoint”
 - “a class is a union (or intersection) of other classes”
 - “a class is a negation of another class”
- *OWL expresses all this and more!*



Basic idea

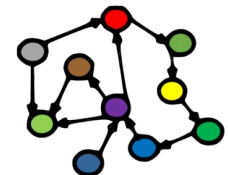
- Web Ontology Language (OWL):
 - *builds* on RDF and RDFS
 - *reuses*, *renames* and *specialises* classes and properties from RDFS
 - *adds* precision and formality
- Basic OWL-concepts:
 - `owl:Thing` (equivalent to `rdfs:Resource`)
 - `owl:Class` (equivalent to `rdfs:Class`)
 - `owl:ObjectProperty` (equivalent to `rdf:Property`)
 - `owl:NamedIndividual` (things with URIs and that are not classes)
- Good practice: keep *Classes*, *Individuals*, and *Properties* disjoint, i.e., no resource has more than one of them as *rdf:type*





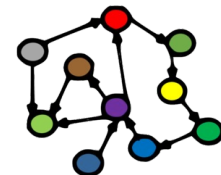
What does OWL offer?

- Extensions of RDFS, e.g.:
 - more *specific types* of properties
 - *identical and different* classes, properties, individuals
 - *defining new classes*:
 - complex classes (union, intersection, complement)
 - property restrictions, enumeration of individuals
 - *defining new properties* based on existing ones
 - *mathematical formality* (for large parts of OWL)
 - (more on this later)



Reuses or specialises RDFS

- *Reused* in OWL:
 - `rdf:type`, `rdf:Property`,
`rdfs:subClassOf`, `rdfs:subPropertyOf`, `rdfs:domain`, `rdfs:range`
 - ...and lots of other stuff...
- *Renamed* by OWL:
 - `owl:Thing` (equivalent to `rdfs:Resource`)
 - `owl:Class` (equivalent to `rdfs:Class`)
 - `owl:ObjectProperty` (equivalent to `rdf:Property`)
- *Specialised* by OWL:
 - everything else in OWL *specialises* something in RDF / RDFS
 - but also introduces its own, and more powerful, formal underpinning

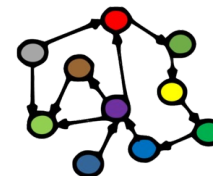


Basic OWL ("RDFS Plus")

Inverse properties

- Properties can be inverses (or reverses) of one another, e.g.,
 - `ex:DonaldTrump ex:presidentOf ex:USA .`
 - `ex:USA ex:hasPresident ex:DonaldTrump .`
- `P1 owl:inverseOf P2`:
 - `ex:presidentOf owl:inverseOf ex:hasPresident .`
 - `owl:inverseOf owl:inverseOf owl:inverseOf .`
 - `owl:inverseOf` a `owl:ObjectProperty` .
- Entailment rules:
 - if *`P1 owl:inverseOf P2`* then
 - *`P2 owl:inverseOf P1 .`*
 - if *`S P1 O . P1 owl:inverseOf P2`* then
 - *`O P2 S .`*

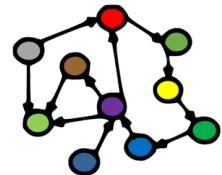
*The axioms
are informative
(not mandatory)*



Symmetric properties

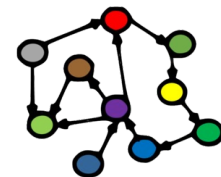
- Some properties are their own inverse, e.g.,
 - `ex:DonaldTrump ex:marriedTo ex:MelianaTrump .`
 - `ex:MelianaTrump ex:marriedTo ex:DonaldTrump .`
- `P rdf:type owl:SymmetricProperty`:
 - `ex:marriedTo a owl:SymmetricProperty .`
 - `owl:inverseOf a owl:SymmetricProperty .`
 - `owl:SymmetricProperty rdfs:subClassOf owl:ObjectProperty .`
- Entailment rules:
 - if *P a `owl:SymmetricProperty`* then
 - *P `owl:inverseOf` P .*
 - if *$S P O$. P a `owl:SymmetricProperty`* then
 - *$O P S$.*

*The axioms
are informative
(not mandatory)*



Asymmetric, reflexive, irreflexive properties

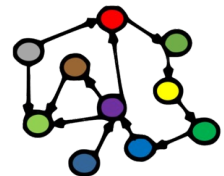
- New in OWL2:
 - both *symmetric* and *asymmetric* properties:
 - ex:marriedTo a owl:SymmetricProperty .
 - “marriage is always mutual (two-way)”
 - ex:hasChild a owl:AsymmetricProperty .
 - “two resources cannot be the child of each other”
 - *many properties are neither – leave it open!*
 - both *reflexive* and *irreflexive* properties:
 - owl:sameAs a owl:ReflexiveProperty .
 - “every resource is the same as itself”
 - ex:hasChild a owl:IrreflexiveProperty .
 - “no resource can be its own child”
 - *many properties are neither – leave it open!*



Transitive properties

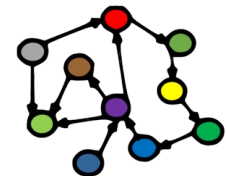
- Some properties can form chains so that the result is the property itself, e.g.:
 - `ex:DonaldTrump ex:hasPredecessor ex:BarackObama .`
 - `ex:BarackObama ex:hasPredecessor ex:GeorgeWBush .`
 - `ex:DonaldTrump ex:hasPredecessor ex:GeorgeWBush .`
- `P a owl:TransitiveProperty:`
 - `ex:hasPredecessor a owl:TransitiveProperty .`
 - `rdfs:subClassOf a owl:TransitiveProperty .`
 - `rdfs:subPropertyOf a owl:TransitiveProperty .`
- Entailment rules:
 - “if $S P X . X P O . P a owl:TransitiveProperty$ then
 - $S P O .$ ”

*The axioms
are informative
(not mandatory)*



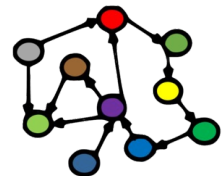
Functional properties

- Each subject *can only have one* object value for the functional property, e.g.,
 - `ex:hasPresident` a `owl:FunctionalProperty` .
 - `ex:dateOfBirth` a `owl:FunctionalProperty` .
 - `owl:FunctionalProperty` `rdfs:subClassOf owl:ObjectProperty` .
- Entailment rule:
 - if $S P O1 . S P O2 . P$ a *owl:FunctionalProperty* then
 - $O1$ *owl:sameAs* $O2$.
 - The rule also holds for *owl:DatatypeProperties*, but:
 - if two different literals become asserted as *owl:sameAs* one another, *the ontology is inconsistent*



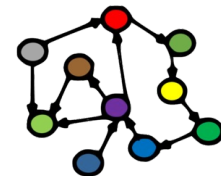
Functional properties

- Each subject *can only have one* object value for the functional property, e.g.,
 - `ex:hasPresident` a `owl:FunctionalProperty` .
 - `ex:dateOfBirth` a `owl:FunctionalProperty` .
 - `owl:FunctionalProperty` `rdfs:subClassOf owl:ObjectProperty` .
- Entailment rule:
 - if $S P O1 . S P O2 . P$ a *owl:FunctionalProperty* then
 - $O1$ *owl:sameAs* $O2$.
 - The rule also holds for *owl:DatatypeProperties*, but:
 - if two different literals become asserted as *owl:sameAs* one another, *the ontology is inconsistent*



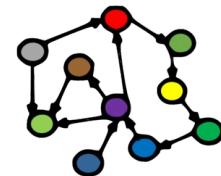
Inverse functional properties

- Two different subjects cannot have the same object for an inverse functional property, i.e.,
 - `ex:presidentOf` a `owl:InverseFunctionalProperty` .
- Entailment rule:
 - if $S1 P O . S2 P O . P$ a *owl:InverseFunctionalProperty* then
 - $S1$ *owl:sameAs* $S2$.
- Inverse functional properties are *unique* for each individual
 - used for *identifiers*
 - OWL 2 also has a built-in *owl:hasKey* property for identifiers



Summary: more precise properties

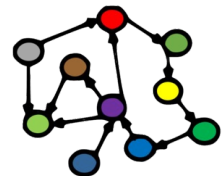
- `owl:inverseOf`
- `owl:SymmetricProperty`, `owl:AsymmetricProperty`
- `owl:ReflexiveProperty`, `owl:IrreflexiveProperty`
- `owl:TransitiveProperty`
- `owl:FunctionalProperty`, `owl:InverseFunctionalProperty`
- `owl:hasKey`
- Also:
 - negated properties
 - chained properties, e.g.:
`fam:hasGrandmother`
`owl:propertyChainAxiom`
`(:hasParent :hasMother)`.



Individual equivalence

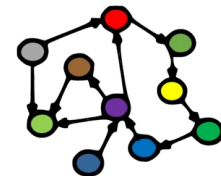
- Sometimes, two individuals (with different URI-s) represent the same thing:
 - http://dbpedia.org/resource/Donald_Trump
 - <http://wikidata.org/entity/Q22686>
- I1 owl:sameAs I2:
 - owl:sameAs a owl:ReflexiveProperty .
 - owl:sameAs a owl:SymmetricProperty .
 - owl:sameAs a owl:TransitiveProperty .
- owl:sameAs is an *equivalence relation*:
 - because it is *reflexive*, *symmetric* and *transitive*

The axioms
are informative
(not mandatory)



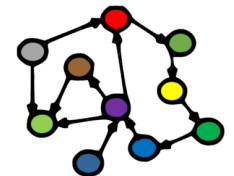
Unique Name Assumption (UNA)

- If two resources have different names, do they necessarily represent different things?
- RDF and OWL does not assume this!
 - *in RDF and OWL, we do not know whether resources with different names represent different things or not*
- We can use
 - `owl:sameAs` – two resources represent the same thing
 - `owl:differentFrom` – they represent different things
 - ...or we can leave it open
- Some ICT-languages and technologies use UNA, others do not!



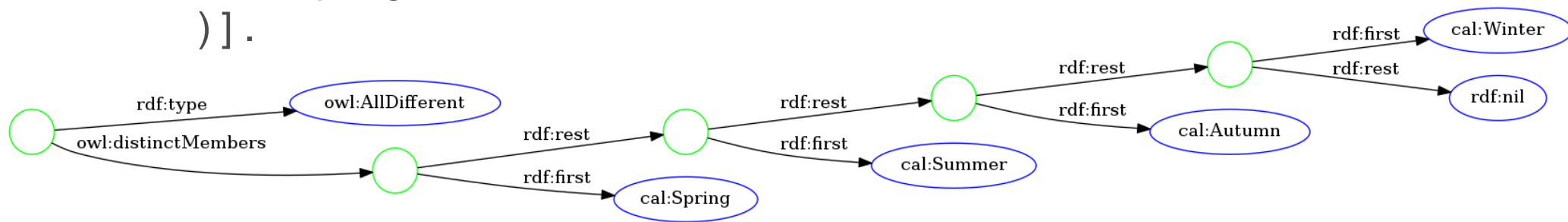
Individual difference

- Sometimes, a *pair* of individuals with different names (URI-s) represent *different* things, e.g.,
 - `cal:Spring owl:differentFrom cal:Summer .`
- `owl:differentFrom`
 - *not* transitive
 - *not* reflexive



Individual difference

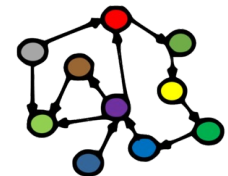
- Sometimes, a pair of individuals with different names (URI-s) represent different things, e.g.,
 - cal:Spring owl:differentFrom cal:Summer .
- Sometimes, a *group* of individuals with different names (URI-s) *all* represent *different* things, e.g.,
 - [a owl:AllDifferent ; owl:distinctMembers (cal:Spring cal:Summer cal:Autumn cal:Winter)] .



Namespaces:
rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
cal: <http://ex.org/cal/>
owl: <http://www.w3.org/2002/07/owl#>

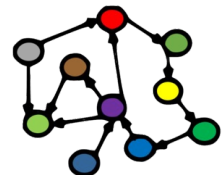
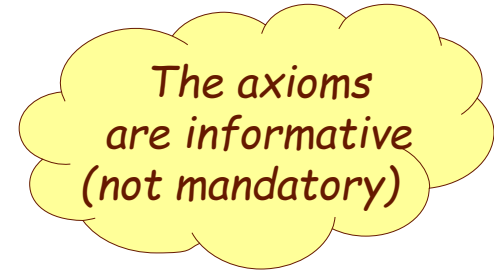
Individual difference

- Sometimes, a pair of individuals with different names (URI-s) represent different things, e.g.,
 - `cal:Spring owl:differentFrom cal:Summer` .
- Sometimes, a group of individuals with different names (URI-s) all represent different things, e.g.,
 - [`a owl:AllDifferent ; owl:distinctMembers (cal:Spring cal:Summer cal:Autumn cal:Winter)`] .
 - *owl:AllDifferent* and *owl:distinctMembers* are special constructs in OWL
 - they must always be used together
 - ...corresponds to pairwise *owl:differentFrom* between *all* individuals in the *owl:distinctMembers*-list



Equivalent classes

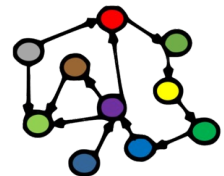
- Sometimes, two classes (with different URI-s) represent the *same* class:
- C1 owl:equivalentClass C2:
 - owl:equivalentClass a owl:ReflexiveProperty .
 - owl:equivalentClass a owl:SymmetricProperty .
 - owl:equivalentClass a owl:TransitiveProperty .
- owl:equivalentClass is another *equivalence relation*:
 - it is *reflexive*, *symmetric* and *transitive*
- C1 owl:equivalentClass C2 means the same as
 - C1 rdfs:subClassOf C2 and C2 rdfs:subClassOf C1
- Also *disjoint* classes:
 - *uib:InternalCensor*
owl:disjointWith skos:ExternalCensor .



Equivalent properties

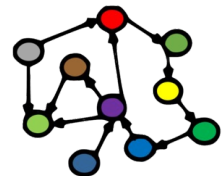
- Two properties (with different URI-s) can represent the same property:
- P1 owl:equivalentProperty P2:
 - owl:equivalentProperty a owl:ReflexiveProperty .
 - owl:equivalentProperty a owl:SymmetricProperty .
 - owl:equivalentProperty a owl:TransitiveProperty .
- owl:equivalentProperty is another *equivalence relation*:
 - it is *reflexive*, *symmetric* and *transitive*
- Also *disjoint* properties:
 - skos:prefLabel owl:propertyDisjointWith skos:altLabel .

The axioms
are informative
(not mandatory)



Summary: sameness and difference

- Individuals:
 - pairwise: `owl:sameAs`, `owl:differentFrom`
 - groupwise difference: `owl:AllDifferent`
- Classes:
 - pairwise: `owl:equivalentClass`, `owl:disjointWith`
 - groupwise difference: `owl:AllDisjointClasses`
- Properties:
 - pairwise: `equivalentProperty`, `propertyDisjointWith`
 - groupwise difference: `owl:AllDisjointProperties`
- Membership in the groups:
 - `owl:distinctMembers` (*preferred*) or `owl:members`



Basic OWL reasoning in Python and rdflib

Basic OWL inference in RDFLib

- `import owlrl`

...

```
DeductiveClosure(RDFS_Semantics).expand(graph) # RDFS reasoning
```

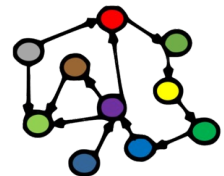
...

```
DeductiveClosure(OWLRL_Semantics).expand(graph) # OWL-RL reasoning
```

...

```
DeductiveClosure(OWLRL_Extension,  
                  rdfs_closure = True, axiomatic_triples = True,  
                  datatype_axioms = True).expand(graph) # Maximum reasoning
```

...

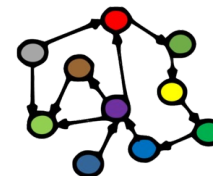


Complex OWL classes

Union classes

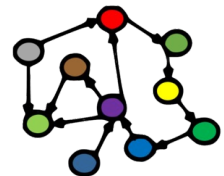
- A union class contains all the individuals in *either of two* or more other classes, e.g.,
 - foaf:Agent
a owl:Class;
owl:unionOf (foaf:Person foaf:Organization) .
- Entailment rule:
 - if *C owl:equivalentClass [owl:unionOf (C1... Cn)]* then
 - *C1 rdfs:subClassOf C Cn rdfs:subClassOf C .*
- why not say just, e.g.,:
 - foaf:Person rdfs:subClassOf foaf:Agent .
 - foaf:Organization rdfs:subClassOf foaf:Agent .

Actually, FOAF defines more types of Agents than this!



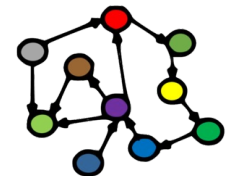
Intersection classes

- An intersection class contains all the individuals in *all of* two or more other classes, e.g.
 - `uib:StudentAssistant`
a `owl:Class`;
`owl:intersectionOf (uib:Student uib:Teacher) .`
- Entailment rule:
 - if *C owl:equivalentClass [owl:intersectionOf (C1... Cn)]* then
 - *C rdfs:subClassOf C1 C rdfs:subClassOf Cn .*
- why not say, e.g.:
 - `uib:StudentAssistant rdfs:subClassOf uib:Student .`
 - `uib:StudentAssistant rdfs:subClassOf uib:Teacher .`



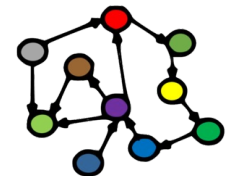
Complement classes

- A complement class contains all the individuals *that are not* in another class:
 - `uib:ExternalCensor owl:complementOf uib:InternalCensor .`



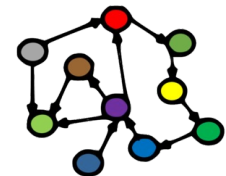
Complement classes

- A complement class contains all the individuals *that are not* in another class:
 - `uib:ExternalCensor owl:complementOf uib:InternalCensor .`
 - *...but is this correct?!*



Complement classes

- A complement class contains all the individuals *that are not* in another class:
 - `uib:ExternalCensor`
 `a owl:Class;`
 `owl:complementOf uib:InternalCensor .`



Complement classes

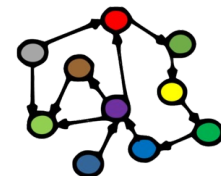
- A complement class contains all the individuals *that are not* in another class:
 - `uib:ExternalCensor`
 - `owl:intersectionOf (`
 - `uib:Censor`
 - `owl:complementOf uib:InternalCensor`



Complement classes

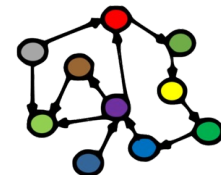
- A complement class contains all the individuals *that are not* in another class:
 - `uib:ExternalCensor`

```
owl:intersectionOf (  
  uib:Censor  
  [  
    a owl:Class ;  
    owl:complementOf uib:InternalCensor  
  ]  
).
```



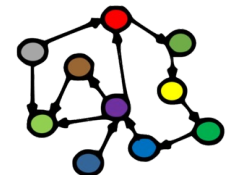
Complement classes

- A complement class contains all the individuals *that are not* in another class:
 - `uib:ExternalCensor`
`owl:intersectionOf (`
 `uib:Censor`
 `[owl:complementOf uib:InternalCensor]`
`)`.



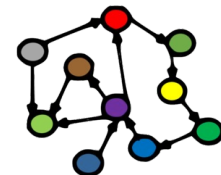
Closed World Assumption (CWA)

- Whenever something is not explicitly stated in the ontology, can we assume that the opposite is the case?
 - DBpedia only lists three James Dean movies – can we thus assume that he only played in three?
- Classical logic and many ICT languages assume so:
 - this is the “*Closed World Assumption*” (CWA)
- *In RDF and OWL, we do not assume that something is false just because it is not stated*
 - this is the “*Open World Assumption*” (OWA)



Enumeration classes

- An *enumeration class* is defined by exhaustively listing all its member individuals, e.g.:
 - [a owl:Class ;
owl:oneOf (cal:Spring ... cal:Winter)] .
- An enumeration class is *closed*
 - there are no other member individuals
 - ensured by using *RDF Collections*:
 - rdf:List, rdf:first, rdf:rest, rdf:nil
- **Does *not* imply** that the individuals are **distinct**
 - this must be stated explicitly



Other ways to write complex classes

- Why can also write:

```
cal:Season
```

```
  owl:oneOf ( cal:Spring ... cal:Winter ) .
```

or

```
cal:Season owl:equivalentClass [
```

```
  owl:oneOf ( cal:Spring ... cal:Winter ) ] .
```

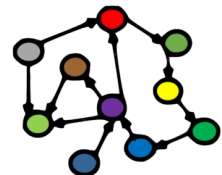
- or (a weaker claim):

```
cal:Season owl:subClassOf [
```

```
  owl:oneOf ( cal:Spring ... cal:Winter ) ] .
```

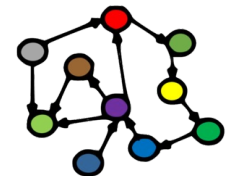
- Reason:

- *rdfs:subClassOf* can be computationally more efficient
- *owl:equivalentClass* is sometimes implemented as a costly two-way *rdfs:subClassOf*



Summary: complex classes

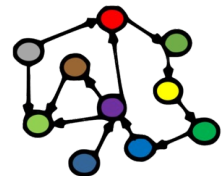
- owl:oneOf
- owl:unionOf
- owl:intersectionOf
- owl:complementOf (and the CWA)
- owl:NegativePropertyAssertion, owl:sourceIndividual, owl:assertionProperty, owl:targetIndividual



OWL restriction classes

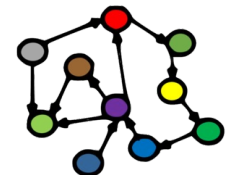
Property value restrictions

- Defining a class by a particular value on one of its properties, e.g.:
 - `ex:Republican`
 - a `owl:Restriction` ;
 - `owl:onProperty` `dbo:hasParty` ;
 - `owl:hasValue` `dbr:Republican_Party_(United_States)` .



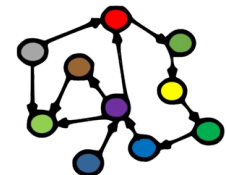
Property value restrictions

- Defining a class by a particular value on one of its properties, e.g.:
 - `ex:Republican owl:intersectionOf (`
 `dbr:Person`
 `[`
 `a owl:Restriction ;`
 `owl:onProperty dbo:hasParty ;`
 `owl:hasValue dbr:Republican_Party_(United_States)`
 `]`
 `) .`



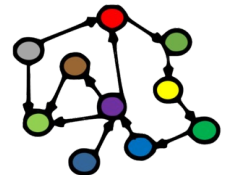
Existential property restrictions

- Defining a class by the existence of a relation (object property) to an individual in (another or the same) class, e.g.:
 - `ex:President owl:intersectionOf (`
 `dbr:Person`
 `[` a owl:Restriction ;
 owl:onProperty `ex:presidentOf` ;
 owl:someValuesFrom owl:Thing
 `]`
 `)` .
- *owl:someValuesFrom*: each individual in the defined class has *at least one* object property (given by owl:onProperty) to an individual in the other class (given by owl:someValuesFrom)



Existential property restrictions

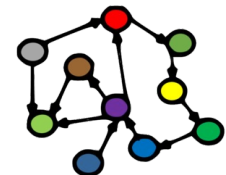
- Defining a class by the existence of a relation (object property) to an individual in (another or the same) class, e.g.:
 - `dbr:President_(government_title) owl:intersectionOf (dbr:Person [a owl:Restriction ; owl:onProperty ex:presidentOf ; owl:someValuesFrom dbr:Nation]) .`
- *owl:someValuesFrom*: each individual in the defined class has *at least one* object property (given by `owl:onProperty`) to an individual in the other class (given by `owl:someValuesFrom`)



Existential property restrictions

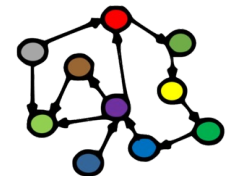
- Defining a class by the existence of a relation (object property) to an individual in (another or the same) class, e.g.:

```
– ex:BipartisanCommittee owl:intersectionOf (  
  foaf:Group  
  [  
    a owl:Restriction ;  
    owl:onProperty foaf:member ;  
    owl:someValuesFrom ex:Republican_(United_States)  
  ]  
  [  
    a owl:Restriction ;  
    owl:onProperty foaf:member ;  
    owl:someValuesFrom ex:Democrat_(United_States)  
  ]  
).
```



Universal property restrictions

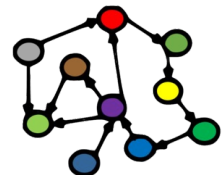
- Defining a class by the necessity of a relation (object property) only to individuals in (another or the same) class, e.g.:
 - `ex:RepublicanCommittee owl:intersectionOf (`
 `foaf:Group`
 `[` `a owl:Restriction ;`
 `owl:onProperty foaf:member ;`
 `owl:allValuesFrom ex:Republican_(United_States)`
 `]`
 `).`



Universal property restrictions

- Defining a class by the necessity of a relation (object property) only to individuals in (another or the same) class, e.g.:
 - `ex:RepublicanCommittee owl:intersectionOf (foaf:Group [a owl:Restriction ; owl:onProperty foaf:member ; owl:allValuesFrom ex:Republican_(United_States)]) .`

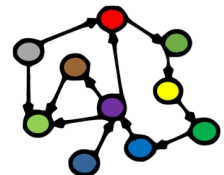
What is wrong here?



Universal property restrictions

- Defining a class by the necessity of a relation (object property) only to individuals in (another or the same) class, e.g.:

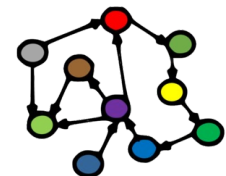
```
– ex:RepublicanCommittee owl:intersectionOf (  
  foaf:Group  
  [  
    a owl:Restriction ;  
    owl:onProperty foaf:member ;  
    owl:allValuesFrom ex:Republican_(United_States)  
  ]  
  [  
    a owl:Restriction ;  
    owl:onProperty foaf:member ;  
    owl:someValuesFrom owl:Thing  
  ]  
).
```



Universal property restrictions

- Defining a class by the necessity of a relation (object property) only to individuals in (another or the same) class, e.g.:

```
– ex:RepublicanCommittee owl:intersectionOf (  
  foaf:Group  
  [  
    a owl:Restriction ;  
    owl:onProperty foaf:member ;  
    owl:allValuesFrom [  
      a owl:Restriction ;  
      owl:onProperty ex:hasParty ;  
      owl:hasValue ex:Republican_Party_(United_States)  
    ]  
  ]  
  [  
    a owl:Restriction ;  
    owl:onProperty foaf:member ;  
    owl:someValuesFrom owl:Thing  
  ]  
  ) .
```

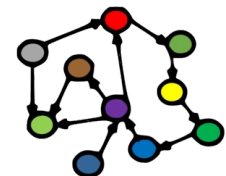


Property self-reflexion

- Defining a class by a *Self* value on one of its properties, e.g.:

- `ex:Narcissist`

```
a owl:Restriction ;  
  owl:onProperty ex:loves ;  
  owl:hasSelf "true"^^xsd:boolean .
```

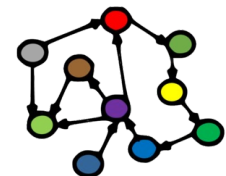


Datatype property restriction

- Restrictions on data range, e.g.:
 - `fam:personAge` `rdfs:range`

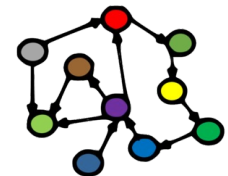
```
[ a rdfs:Datatype;  
  owl:onDatatype xsd:integer;  
  owl:withRestrictions (  
    [ xsd:minInclusive "0"^^xsd:integer ]  
    [ xsd:maxInclusive "130"^^xsd:integer ] )  
  ].
```
 - `:toddlerAge` `rdfs:range`

```
[ a rdfs:Datatype;  
  owl:oneOf ( "1"^^xsd:integer "2"^^xsd:integer )  
  ].
```



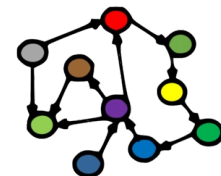
Cardinality restriction

- Defining a class by the number of object values its individuals have for some property, e.g.:
 - `music:Quartet` owl:intersectionOf (
 `music:Ensemble`
 [owl:Restriction ;
 owl:onProperty `music:hasMusician` ;
 owl:cardinality 4]
) .
- `owl:cardinality` gives the *exact cardinality*
`owl:minCardinality` gives the *least cardinality*
`owl:maxCardinality` gives the *greatest cardinality*



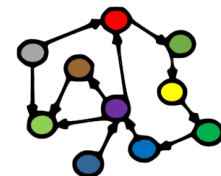
Qualified cardinality restriction

- Defining a class by the number of object values its individuals have of a *given class* for some property, e.g.:
 - `pol:Triumvirate owl:intersectionOf (`
 `pol:PoliticalLeadership`
 `[` a `owl:Restriction ;`
 `owl:onProperty pol:hasMember ;`
 `owl:qualifiedCardinality 3 ;`
 `owl:onClass pol:PoliticalLeader` `]`
 `) .`
- `owl:qualifiedCardinality` gives the *exact cardinality*
`owl:minQualifiedCardinality` gives the *least cardinality*
`owl:maxQualifiedCardinality` gives the *greatest cardinality*



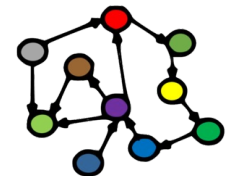
Qualified cardinality restriction

- `music:StringQuartet` owl:intersectionOf (
 - `music:MusicalQuartet`
 - [a owl:Class ;
owl:onProperty `music:hasMusician` ;
owl:qualifiedCardinality "2" ;
owl:onClass `music:Violinist`]
 - [a owl:Class ;
owl:onProperty `music:hasMusician` ;
owl:qualifiedCardinality "1" ;
owl:onClass `music:Violist`]
 - [a owl:Class ;
owl:onProperty `music:hasMusician` ;
owl:qualifiedCardinality "1" ;
owl:onClass `music:Cellist`]) .



Summary: property restrictions

- owl:Restriction owl:onProperty
- owl:someValuesFrom, owl:allValuesFrom, owl:hasValue
- owl:cardinality, owl:minCardinality, owl:maxCardinality
- owl:qualifiedCardinality, owl:minQualifiedCardinality, owl:maxQualifiedCardinality, owl:onClass



**Next week:
Vocabularies**